



Dynamical Paleoclimatology

***Generalized Theory of
Global Climate Change***

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Global Climate Change

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J III 98

DK. 551.583.7, 551.583

347/4177

INSTITUT

FÜR METEOROLOGIE U. KLIMATOLOGIE

UNIVERSITÄT HANNOVER

HERRENHÄUSER STR. 2 - 30419 HANNOVER



ACADEMIC PRESS

A Harcourt Science and Technology Company

San Diego San Francisco New York Boston London Sydney Tokyo

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