



A First  
Course In  
**Atmospheric  
Radiation**

Second Edition

Grant W. Petty

**A First Course in**

# **Atmospheric Radiation**

**Second Edition**

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## Contents

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<b>Preface to the Second Edition</b>	<b>iii</b>
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<b>Preface to the First Edition</b>	<b>v</b>
-------------------------------------	----------

<b>1 Introduction</b>	<b>1</b>
1.1 Relevance for Climate and Weather . . . . .	1
1.1.1 Solar Radiation . . . . .	2
1.1.2 Thermal Infrared Radiation . . . . .	3
1.1.3 The Global Heat Engine . . . . .	4
1.1.4 Components of the Earth's Energy Budget . . . . .	6
1.2 Relevance for Remote Sensing . . . . .	7
<b>2 Properties of Radiation</b>	<b>11</b>
2.1 The Nature of Electromagnetic Radiation . . . . .	11
2.2 Frequency . . . . .	16
2.2.1 Frequency Decomposition . . . . .	18
2.2.2 Broadband vs Monochromatic Radiation . . . . .	19
2.3 Polarization . . . . .	20
2.4 Energy . . . . .	22
2.5 A Mathematical Description of EM Waves <sup>†</sup> . . . . .	24
2.6 Quantum Properties of Radiation . . . . .	31
2.7 Flux and Intensity . . . . .	33
2.7.1 Flux . . . . .	33

2.7.2	Intensity . . . . .	35
2.7.3	Relationship between Flux and Intensity . . . . .	46
2.8	Applications . . . . .	49
2.8.1	Global Insolation . . . . .	49
2.8.2	Regional and Seasonal Distribution of Insolation	50
<b>3</b>	<b>The Electromagnetic Spectrum</b>	<b>55</b>
3.1	Frequency, Wavelength and Wavenumber . . . . .	56
3.2	Major Spectral Bands . . . . .	57
3.2.1	Gamma Rays and X-Rays . . . . .	61
3.2.2	Ultraviolet Band . . . . .	61
3.2.3	Visible Band . . . . .	63
3.2.4	Infrared Band . . . . .	64
3.2.5	Microwave and Radio Bands . . . . .	66
3.3	Solar and Terrestrial Radiation . . . . .	68
3.4	Applications . . . . .	69
3.4.1	UV Radiation and Ozone . . . . .	69
<b>4</b>	<b>Reflection and Refraction</b>	<b>74</b>
4.1	A Closer Look at $N$ . . . . .	76
4.1.1	The Real Part . . . . .	76
4.1.2	The Imaginary Part . . . . .	76
4.1.3	The Dielectric Constant <sup>†</sup> . . . . .	79
4.1.4	Optical Properties of Heterogeneous Mixtures <sup>†</sup>	80
4.2	Refraction and Reflection . . . . .	82
4.2.1	Angle of Reflection . . . . .	82
4.2.2	Angle of Refraction . . . . .	84
4.2.3	Reflectivity . . . . .	86
4.3	Applications . . . . .	90
4.3.1	Rainbows and Halos . . . . .	90
<b>5</b>	<b>Radiative Properties of Natural Surfaces</b>	<b>96</b>
5.1	Natural Surfaces Idealized as Planar Boundaries . . . . .	97
5.2	Absorptivity and Reflectivity . . . . .	98
5.2.1	Examples of Reflectivity Spectra . . . . .	99
5.2.2	The Graybody Approximation . . . . .	100
5.3	Angular Distribution of Reflected Radiation . . . . .	102
5.3.1	Specular and Lambertian Reflection . . . . .	102
5.3.2	Reflection in the General Case <sup>†</sup> . . . . .	105

5.4 Applications . . . . .	107
5.4.1 Solar Heating of Surfaces . . . . .	107
5.4.2 Satellite Imaging at Visible and Near-IR Wavelengths . . . . .	109
<b>6 Thermal Emission</b>	<b>113</b>
6.1 Blackbody Radiation . . . . .	115
6.1.1 Planck's Function . . . . .	117
6.1.2 Wien's Displacement Law . . . . .	120
6.1.3 Stefan-Boltzmann Law . . . . .	122
6.1.4 Rayleigh-Jeans Approximation . . . . .	123
6.2 Emissivity . . . . .	123
6.2.1 Monochromatic Emissivity . . . . .	124
6.2.2 Graybody Emissivity . . . . .	124
6.2.3 Kirchhoff's Law . . . . .	125
6.2.4 Brightness Temperature . . . . .	127
6.3 When Does Thermal Emission Matter? . . . . .	130
6.4 Applications . . . . .	132
6.4.1 Radiative Equilibrium in a Vacuum . . . . .	133
6.4.2 Top-of-the-Atmosphere Global Radiation Balance . . . . .	136
6.4.3 Simple Radiative Models of the Atmosphere .	139
6.4.4 Nighttime Radiative Cooling . . . . .	144
6.4.5 Radiative Cooling at Cloud Top . . . . .	146
6.4.6 IR Imaging from Space . . . . .	148
6.4.7 Microwave Imaging from Space . . . . .	151
<b>7 Atmospheric Transmission</b>	<b>155</b>
7.1 Extinction, Scattering and Absorption Coefficients . .	159
7.2 Extinction Over a Finite Path . . . . .	160
7.2.1 Fundamental Relationships . . . . .	160
7.2.2 Mass Extinction Coefficient . . . . .	163
7.2.3 Extinction Cross-Section . . . . .	166
7.2.4 Generalization to Scattering and Absorption .	167
7.2.5 Generalization to Arbitrary Mixtures of Components . . . . .	168
7.3 Plane Parallel Approximation . . . . .	169
7.3.1 Definition . . . . .	171
7.3.2 Optical Depth as Vertical Coordinate . . . . .	173

12.3.1	Extinction Efficiency for Nonabsorbing Sphere	359
12.3.2	Extinction and Scattering by Absorbing Spheres	363
12.3.3	Scattering Phase Function . . . . .	365
12.4	Distributions of Particles . . . . .	372
12.5	Applications . . . . .	373
12.5.1	The Scattering Properties of Clouds . . . . .	373
12.5.2	Radar Observations of Precipitation . . . . .	375
12.5.3	Microwave Remote Sensing and Clouds . . . . .	381
<b>13</b>	<b>Radiative Transfer with Multiple Scattering</b>	<b>387</b>
13.1	Visualizing Multiple Scattering . . . . .	389
13.2	The Two-Stream Method . . . . .	392
13.2.1	Azimuthally Averaged RTE . . . . .	392
13.2.2	The Two-Stream Approximation . . . . .	393
13.2.3	Solution . . . . .	398
13.3	Semi-Infinite Cloud . . . . .	400
13.3.1	Albedo . . . . .	401
13.3.2	Flux and Heating Rate Profile . . . . .	404
13.4	Nonabsorbing Cloud . . . . .	406
13.5	General Case . . . . .	408
13.5.1	Albedo, Transmittance, and Absorptance . . .	409
13.5.2	Direct and Diffuse Transmittance . . . . .	412
13.5.3	Semi-Infinite Cloud as Approximation . . . . .	414
13.6	Similarity Transformations <sup>†</sup> . . . . .	416
13.7	Clouds Over Non-Black Surfaces . . . . .	418
13.8	Multiple Cloud Layers . . . . .	423
13.9	Accurate solution methods <sup>†</sup> . . . . .	424
<b>A</b>	<b>Representing the Phase Function</b>	<b>427</b>
A.1	Legendre Polynomial Expansion . . . . .	427
A.2	$\delta$ -Scaling of the Phase Function . . . . .	430
<b>B</b>	<b>Symbols Used</b>	<b>438</b>
<b>C</b>	<b>Further Reading</b>	<b>445</b>
<b>D</b>	<b>Useful Physical and Astronomical Constants</b>	<b>447</b>
	<b>Ordering Information</b>	<b>459</b>