



# Synoptic–Dynamic Meteorology in Midlatitudes

VOLUME I

Principles of Kinematics and Dynamics

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# Contents

## 1. INTRODUCTION 3

- 1.1 What is Synoptic Meteorology? 3**
  - 1.1.1 Historical background 3
  - 1.1.2 Classification of atmospheric phenomena 5
  - 1.1.3 Atmospheric phenomena as fractals 7
  - 1.1.4 The role of observations and theory 7
  - 1.1.5 The mystery of synoptic meteorology 11
  - 1.1.6 The organization of this text 15
- 1.2 Units and Variables 15**
  - 1.2.1 The MKS system 15
  - 1.2.2 The MTS system 16
  - 1.2.3 Other useful conversion factors 17
- 1.3 Coordinate Systems 17**
  - 1.3.1 Cartesian coordinates 17
  - 1.3.2 Natural coordinates 18
  - 1.3.3 The representation of the wind field 19
  - 1.3.4 Pressure coordinates 21
  - 1.3.5 Isentropic coordinates 22
  - 1.3.6  $\sigma$  coordinates 24
  - 1.3.7 Invariance 25
  - 1.3.8 The total derivative 25

**Note 28**

**References 28**

## 2. SCALAR FIELDS AND THEIR KINEMATICS 32

- 2.1 The Pressure (Height) Field 32**
  - 2.1.1 What is kinematics? 32
  - 2.1.2 A description of features in the pressure (height) field 33
  - 2.1.3 Analysis of the pressure (height) field 43
  - 2.1.4 Kinematics of the pressure (height) field 47
  - 2.1.5 The hydrostatic equation and the reduction of pressure to a reference level 57
- 2.2 The Temperature and Moisture Fields 64**
- 2.3 The Measurement of Scalar Fields 64**
  - 2.3.1 Introduction 64
  - 2.3.2 The measurement of pressure 68
  - 2.3.3 The measurement of height 68

- 2.3.4 The measurement of temperature 68
- 2.3.5 The measurement of humidity 69
- 2.3.6 Clouds 70
- 2.3.7 The measurement of precipitation 70
- 2.3.8 Instrument platforms 73

**Notes** 74

**References** 74

**Problems** 77

### **3. KINEMATICS OF THE WIND FIELD 81**

- 3.1 Properties of the Horizontal Wind Field 81**
  - 3.1.1 The decomposition of a linear wind field 81
  - 3.1.2 Translation 87
  - 3.1.3 Divergence 87
  - 3.1.4 Vorticity 92
  - 3.1.5 Deformation 99
  - 3.1.6 Summary 107
  - 3.1.7 Trajectories 109
- 3.2 The Computation of Divergence, Vorticity, and Deformation 113**
  - 3.2.1 The expressions for divergence, vorticity, and deformation on the Earth's surface 113
  - 3.2.2 Finite-difference computations 114
  - 3.2.3 Integral computations of divergence, vorticity, and deformation 120
  - 3.2.4 The linear vector point function method 123
- 3.3 Properties of the Three-Dimensional Wind Field 124**
- 3.4 Measuring the Wind Field 129**
  - 3.4.1 Introduction 129
  - 3.4.2 Wind-measuring instruments: Dependence of the properties of an object upon wind speed 131
  - 3.4.3 Wind-measuring instruments: The tracking of tracers moving with the horizontal component of the wind 132

**Notes** 146

**References** 146

**Problems** 148

### **4. ELEMENTARY ATMOSPHERIC DYNAMICS AND THERMODYNAMICS 153**

- 4.1 The Law of Motion 153**
  - 4.1.1 The equation of fluid motion on a rotating sphere: Vector form 153

4.1.2	The equations of fluid motion on a rotating sphere: Scalar form	162
4.1.3	The geostrophic wind	171
4.1.4	The isallobaric wind and the inertial–advective wind	173
4.1.5	The equations of motion in natural coordinates	175
4.1.6	The thermal wind	182
<b>4.2</b>	<b>The Equation of Continuity</b>	<b>190</b>
4.2.1	The equation of continuity in height coordinates	190
4.2.2	The equation of continuity in pressure coordinates	192
4.2.3	The equation of continuity in isentropic coordinates	193
4.2.4	The kinematic boundary condition	194
4.2.5	The dynamic boundary condition	195
<b>4.3</b>	<b>The Thermodynamic Equation</b>	<b>195</b>
4.3.1	Dry thermodynamics	195
4.3.2	Moist thermodynamics	200
<b>4.4</b>	<b>Friction</b>	<b>224</b>
4.4.1	Molecular friction	224
4.4.2	Turbulent friction	228
4.4.3	The surface boundary layer	234
4.4.4	The friction layer	236
4.4.5	The turbulent transport of general quantities	244
4.4.6	The antitriptic wind	247
<b>4.5</b>	<b>The Vorticity Equation</b>	<b>247</b>
4.5.1	Derivation of the vorticity equation in height coordinates	247
4.5.2	The Bjerknes and Kelvin circulation theorems	251
4.5.3	Physical interpretation of the vorticity equation and the circulation theorems	254
4.5.4	The vorticity equation in pressure coordinates	259
4.5.5	The vorticity equation in isentropic coordinates and Ertel's potential vorticity	262
4.5.6	The horizontal vorticity equation	268
4.5.7	The three-dimensional vorticity equation in a compressible atmosphere	270
<b>4.6</b>	<b>Energetics</b>	<b>272</b>
<b>4.7</b>	<b>Thermodynamic Retrieval</b>	<b>275</b>
<b>References</b>		<b>277</b>
<b>Problems</b>		<b>280</b>

- 5. QUASIGEOSTROPHIC THEORY 282**
- 5.1 Introduction 282**
- 5.2 Estimating the Terms in the Vorticity and Thermodynamic Equations 285**
- 5.2.1 Substitution of the analytical-model equations into the vorticity and thermodynamic equations 286
- 5.2.2 The relationship between  $w$  and  $\omega$  296
- 5.2.3 The kinematic boundary conditions for midlatitude, synoptic-scale systems 301
- 5.2.4 A simplified vorticity equation 303
- 5.2.5 The thermodynamic equation for synoptic-scale systems in the midlatitudes 305
- 5.2.6 The effects of diabatic heating and static stability 306
- 5.3 Estimating Vertical Motion from the Observed Wind and Mass Fields 313**
- 5.3.1 The kinematic method 313
- 5.3.2 The adiabatic method 316
- 5.3.3 The vorticity method 319
- 5.3.4 Satellite infrared photograph technique 320
- 5.4 Estimating Local Height Tendencies from the Observed Wind and Mass Fields 320**
- 5.5 The Quasigeostrophic Vorticity and Thermodynamic Equations 323**
- 5.5.1 The quasigeostrophic approximation 323
- 5.5.2 The quasigeostrophic vorticity and thermodynamic equations 325
- 5.5.3 The quasigeostrophic equations of motion 327
- 5.6 Derivation of the Quasigeostrophic  $\omega$  and Height-tendency Equations 327**
- 5.6.1 The quasigeostrophic vorticity and thermodynamic equations expressed in terms of the height field 327
- 5.6.2 The quasigeostrophic  $\omega$  equation 328
- 5.6.3 The quasigeostrophic height-tendency equation 329
- 5.6.4 The quasigeostrophic  $\omega$  equation and height-tendency equation with diabatic heating and friction 330
- 5.7 Interpretation of the Quasigeostrophic  $\omega$ -Equation 331**
- 5.7.1 Mathematical interpretation 331
- 5.7.2 Physical interpretation 338
- 5.7.3 The Trenberth formulation of the quasigeostrophic  $\omega$  equation 346
- 5.7.4 The  $\mathbf{Q}$ -vector representation of the quasigeostrophic  $\omega$  equation 350

5.7.5	Comparison of the different quasigeostrophic $\omega$ equations	368
<b>5.8</b>	<b>The Quasigeostrophic Potential Vorticity Form of the Height-Tendency Equation</b>	<b>370</b>
<b>5.9</b>	<b>Static-Stability Effects on Vertical Motion</b>	<b>373</b>
5.9.1	The effects of horizontal variations in static stability on vertical motion	373
5.9.2	Effective static stability	379
<b>5.10</b>	<b>Interpretation of the Quasigeostrophic Height-Tendency Equation</b>	<b>385</b>
5.10.1	Mathematical interpretation	385
5.10.2	Physical interpretation	386
<b>5.11</b>	<b>The Effects of Vertical Variations in Static Stability on the Geopotential-Height Tendency</b>	<b>389</b>
<b>Note</b>		<b>390</b>
<b>References</b>		<b>390</b>
<b>Problems</b>		<b>395</b>
<b>Selected Answers to Problems</b>		<b>404</b>
Appendix 1.	Review of Vector Notation	411
Appendix 2.	Implications of Hydrostatic Balance for the Horizontal and Vertical Scales of Meteorological Phenomena	413
Appendix 3.	Matrix Notation	419
Index		423