



An introduction to  
**DYNAMIC  
METEOROLOGY**

FOURTH EDITION

James R. Holton



# **AN INTRODUCTION TO DYNAMIC METEOROLOGY**

**Fourth Edition**

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