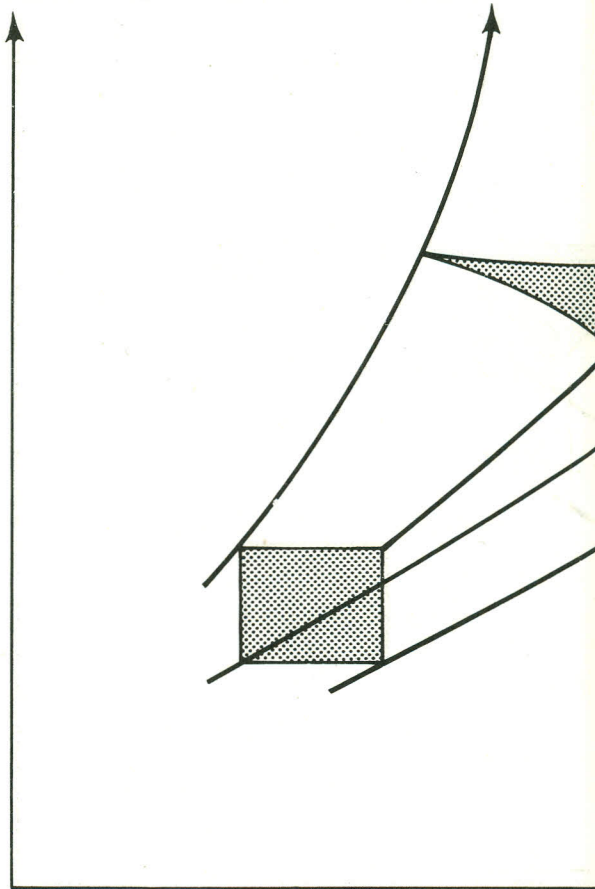


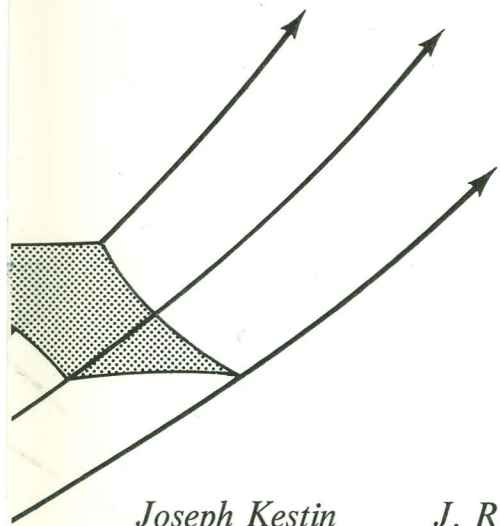
**A COURSE
IN STATISTICAL
THERMODYNAMICS**

Joseph Kestin/J. R. Dorfman

A COURSE IN



STATISTICAL THERMODYNAMICS



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