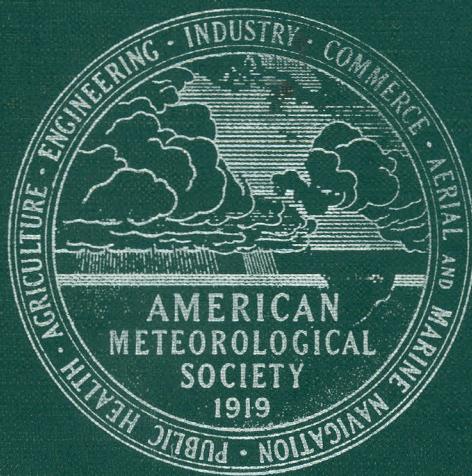


# WORKSHOP on MICROMETEOROLOGY

DUANE A. HAUGEN, EDITOR



American Meteorological Society

# **Workshop on Micrometeorology**

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