

Fluid
Mechanics
and
Thermodynamics
of Our Environment

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FLUID MECHANICS AND THERMODYNAMICS OF OUR ENVIRONMENT

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