

An Introduction to
**Atmospheric
Gravity Waves**



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AN
INTRODUCTION TO
ATMOSPHERIC
GRAVITY WAVES

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