

FLUID MECHANICS AND ITS APPLICATIONS

Sheldon I. Green (Ed.)

Fluid Vortices



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Fluid Vortices

Edited by

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