

Applied Mathematics and  
Mathematical Computation 6

# Vortex Structures in a Stratified Fluid

Order from chaos

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CHAPMAN & HALL

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