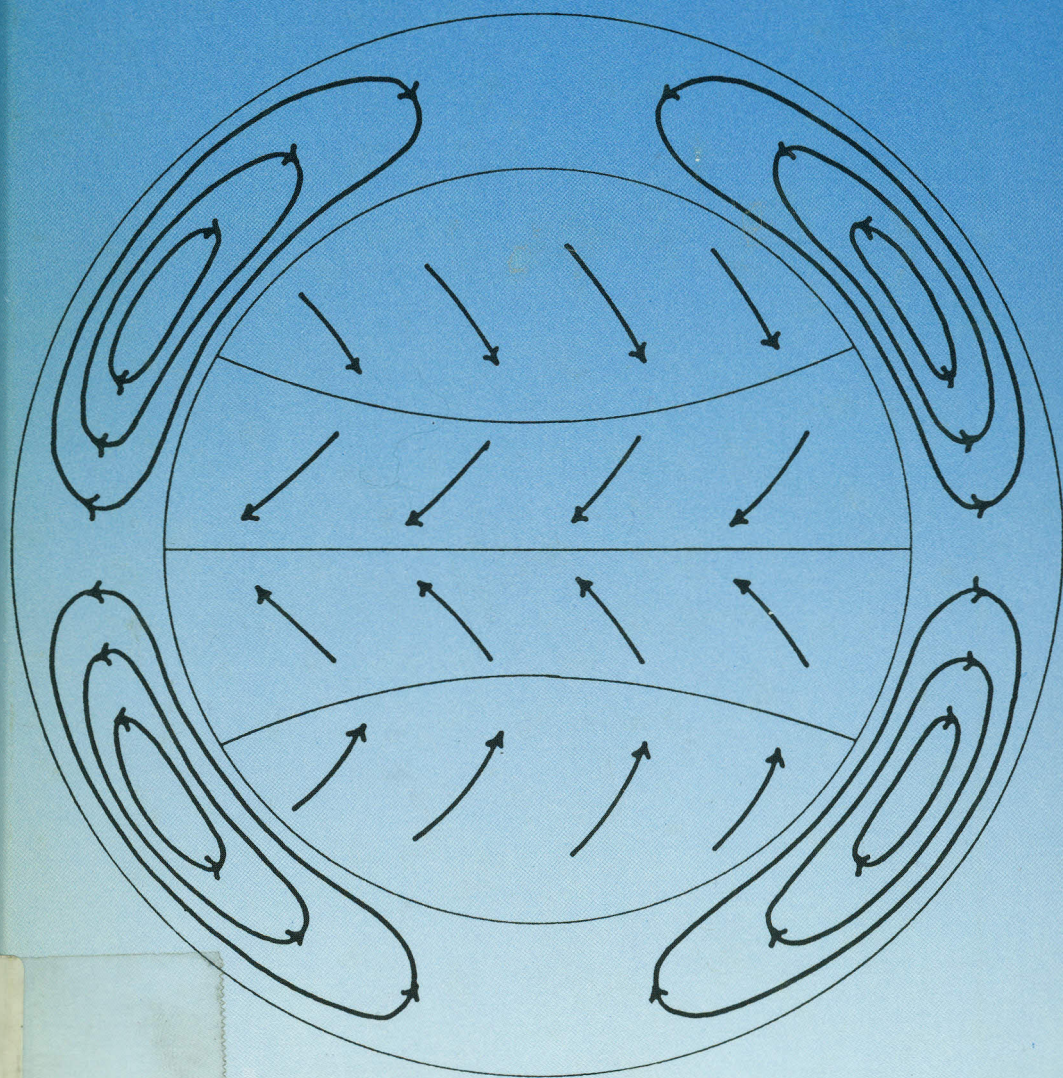


dynamics in Atmospheric Physics



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Dynamics in Atmospheric Physics

Lecture Notes for an Introductory Graduate-Level Course

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