

The background of the book cover is a black and white photograph of a landscape. In the foreground, there are dark, silhouetted trees and a rocky outcrop on the right side. The middle ground shows a valley with a winding path or road. The sky is filled with soft, horizontal clouds, suggesting a misty or overcast day. The overall mood is serene and atmospheric.

FLUID  
MECHANICS  
*of the*  
ATMOSPHERE  
Robert A. Brown

# Fluid Mechanics of the Atmosphere

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