# TURBULENCE and random processes in fluid mechanics



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## Turbulence and random processes in fluid mechanics

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