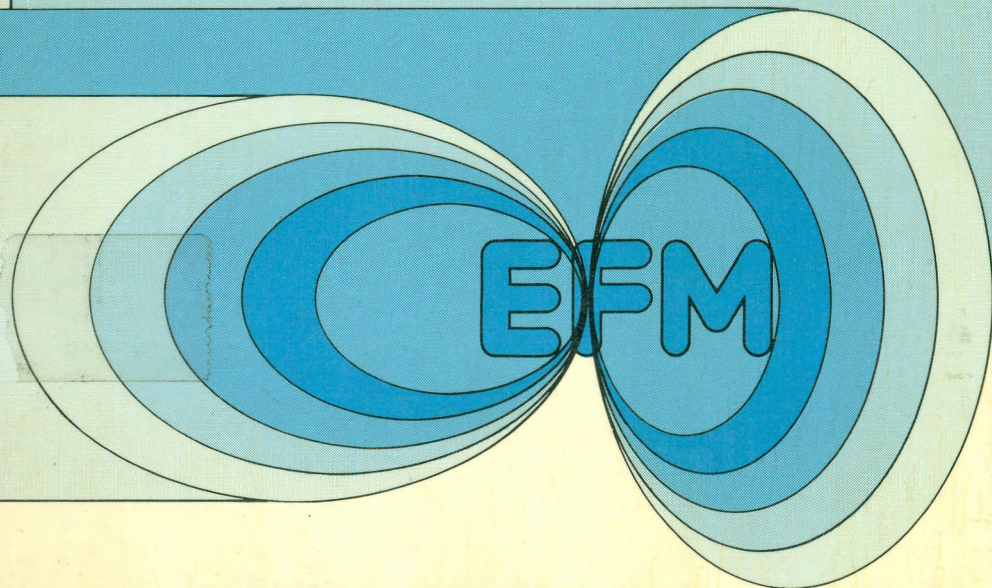


Dynamic Meteorology

S. Panchev

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INSTITUT
FÜR METEOROLOGIE U. KLIMATOLOGIE
UNIVERSITÄT HANNOVER
HERRENHAUSER STR. 2 · 3000 HANNOVER 21

S. PANCHEV

*Department of Meteorology and Geophysics,
University of Sofia, Bulgaria*

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