

# AIR POLLUTION MODELING

Theories, Computational Methods  
and Available Software

Paolo Zannetti



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## Theories, Computational Methods and Available Software

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